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ESTIMATION OF BEARING CAPACITY OF SLOPES STRENGTHENED BY GEOTEXTILES, AND EXPERIMENTAL EXAMINATION

The authors of the article develop the calculation methods of slopes strengthened by geotextile. The received theoretical estimates of bearing capacity are compared with the experimental maximum loads obtained in tray model experiments.

K e y w o r d s: soil slopes, geotextile, bearing capacity, experimental testing.

Constructions and their natural basement must correspond to limiting state and accepted both in Russia and abroad. For instance, Eurocode 7 requires calculation in accordance with “Ultimate Limit States” (ULS) and “Serviceability Limit States” (SLS). There are no reasons to change such approach and in calculations of plastic systems “a soil file — a flexible shell” or soil files reinforced by geosynthetics.

Normative building documents confirm that calculation based on one of limiting states is neither reduced nor replaced with that based on other limiting state.

Calculation of the soil basement reinforced by geosynthetics, based on SLS, i. e. on deformations, does not cause any difficulties [1, 2]. The elastic model of environment and a method of finite elements for calculation the stress and the deformation of a soil file is generally used. Distinctions consist in a degree of the monitoring reinforcing layers of geosynthetics. In one case there are requirements for the increased size of the module of deformation of a soil, for example, $E = 20 \text{ MPa}$. In other case environment is taken as composite, and equivalent rigidity of the reinforced is defined by elastic characteristics of geosynthetics and soil. An option of soil environment being represented by flat triangular elements, and reinforcing geosynthetics by linear elements cooperating with triangular elements is possible to imagine too.

However, calculation of bearing capacity, based on ULS, cannot be executed within elastic model since the latter is not suitable for the description of environment destruction process.

Currently, the applied methods of calculation of building systems “a soil file — flexible geomaterials”, especially on bearing capacity, are represented absolutely unpersuasive. The designer cannot specify by how many percent the bearing capacity of a structure increases after expensive synthetic materials being applied.

Nevertheless, poor development of calculation methods based on ULS leads to replacement of the above calculation with an indirect one, based on calculation of deformations, using some experimental data. Theoretically it means the substitution of calculation based on ULS with calculation on SLS.

According to the marginal analysis of plastic bodies statically admissible field of stress in a slope generates the bottom estimation of limit value of external forces. For a weightless slope the bottom estimation of limit allocated load P is given in the generalized Prandtl's solution being a combination of accurate analytical solutions: the passive elementary limit stress state in field I, simple centered wave in field II and the active elementary limit stress state in field III.

Bearing capacity of a weightless slope under strength of soil

$$\sigma_2 = -C + A\sigma_1 \quad (1)$$

is defined from the following formula

$$P = Ae^{\left(\frac{\pi}{2}-\alpha\right)\frac{A-1}{\sqrt{A}}}\left(q + \frac{C}{A-1}\right) - \frac{C}{A-1}. \quad (2)$$

If corner α is equal to zero, then the (2) allows to derive limit intensity of strip load on natural basement.

When studying the bearing capacity of the composite basement made from condensed gravel and sand mix, homogeneously interlaid with horizontal layers of geosynthetics (for example, texpall) model of a continuous rigidly-ideally-plastic body, anisotropic on resistance to shear strength, is offered to use.

For calculation of bearing capacity of basement in question solution for limit strip loads on anisotropic on resistance of shear strength the soil basement is used [3—5].

Thus, the traditional concept of the strength, based on sliding platforms is changed.

Let us consider any representative volume of the composite basement (fig. 1), being in limit stress state of soil. If this volume is located in zone with active limit stress of soil III (fig. 1, a), then the presence of geosynthetics layers perpendicular to the first mainstream, will not lead to any noticeable hardening of this volume of soil. If this volume is located in zone with passive limit stress of soil I (fig. 1, b), then the presence of geosynthetics layers parallel to the first mainstream, will considerably strengthen this volume of soil depending on rupture strength value of geosynthetics.

Have any representation volume of the basement, the sides of which coincide with the main platforms, placed in the field of the centered wave II. The corner between the first mainstream and geosynthetics layers will be equal to $\pi/2 - \theta$ and change from $\pi/2$ up to 0 on area II. The issue of increasing the strength of the soil environment volume reinforced with inclined layers of geosynthetics can be investigated experimentally.

Let us suggest a hypothesis about linear dependence of strength characteristics A and C from corner θ . Meanwhile, strength characteristics in the field III are accepted as for soil without geosynthetics. In field I to the soil intercept cohesion the "equivalent" cohesion calculated as the ratio of geosynthetics rupture force to the corresponding area, is to be added.

Take, for example, a basement made from gravel and sand mix, having no cohesion, horizontal layers of the stabitex being interlaid through each meter. The rupture limit of a meter stabitex strip is 80 kN. Hence, in this case in field I there will appear "equivalent" cohesion $c = 80 \text{ kN/m}^2$.

Have the slope strengthened by periodic horizontal geosynthetics layers. In the same way like transition from generalized Prandtl's solution for isotropic under resistance to shift of soil half-space to the solution for anisotropic soil half-space is made, we shall make transformation for slope too. Instead of the (2) for bearing capacity of weightless isotropic slope we shall receive algorithm for calculation of bearing capacity of the reinforced slope (fig. 2).

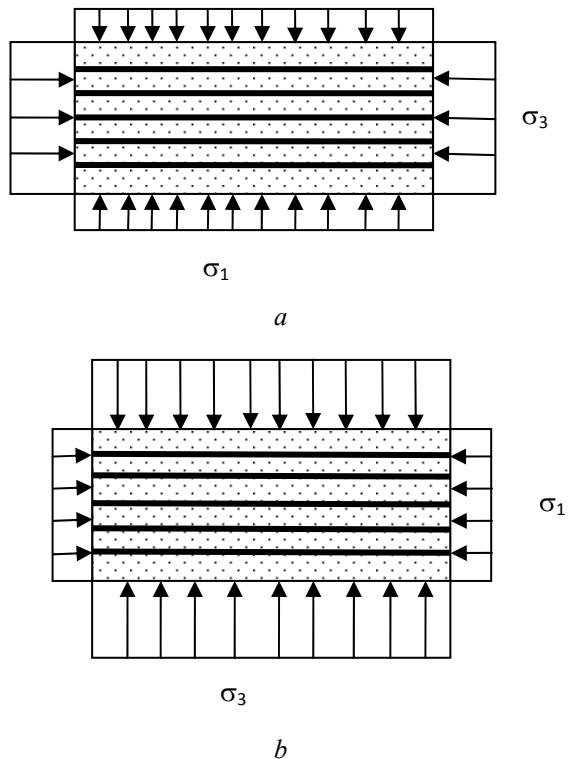


Fig. 1. To the concept of durability of the composite environment

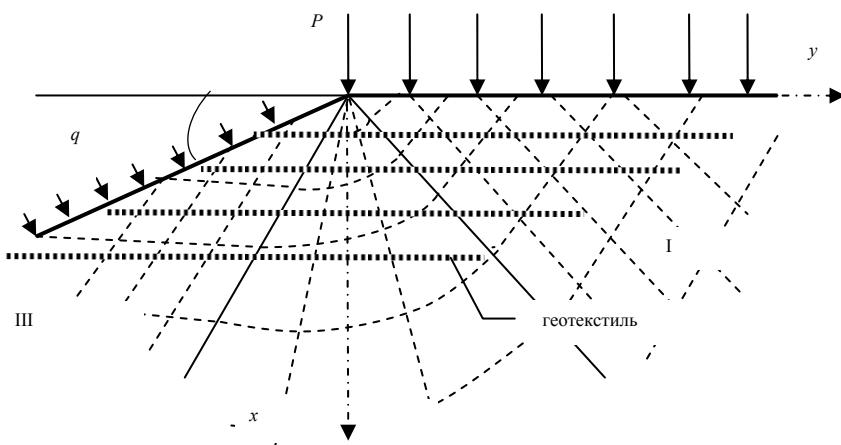


Fig. 2. A limit stress of the weightless slope strengthened by geosynthetics

In case of slope in field III, corner of the first mainstream with axis $OX \theta = \alpha$. Strength characteristics are constant through this area and equal $A(\alpha)$ and $C(\alpha)$.

It is shown [6], which calculation of bearing capacity of the reinforced weightless slope comes to solution of the nonlinear differential equation of the first order.

Remark. Applying famous approached method by Sokolovsky, influence of soil weight on bearing capacity value is possible to consider. Fig. 3 illustrates the above method. With corners α , being smaller then internal friction corner, to allocated load P certain triangular pressure diagram will be added, and with bigger corners α — subtracted. We shall notice that total load will be also the bottom estimation of unknown bearing capacity of slope.

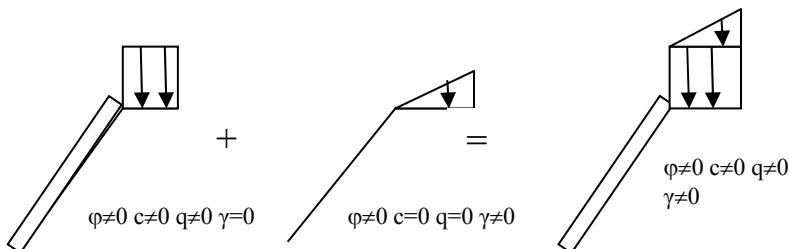


Fig. 3. Sokolovsky's method

To check the operation of the developed estimations of limit load slope modeling tray tests have been carried out.

To study sand basements under flat deformation a tester was designed. Subsequently, to study the operation of foundations models on slope, the tester has been modified. The tester (fig. 4) consists of tray, made of organic glass with 30 mm thickness. A working part of the tray has the sizes $800 \times 105 \times 600$ mm ($L \times B \times H$). The loading device is equipped with two hinges to eliminate kinematic moving restrictions of the foundation model. Load on the foundation model was “dead” and was created by metal disks in weight of three kg each. The sand of average coarse in dense dry air condition (density $\rho = 1,75$ g/sm³, factor of porosity $e = 0,53$) was used for modeling the soil basement.

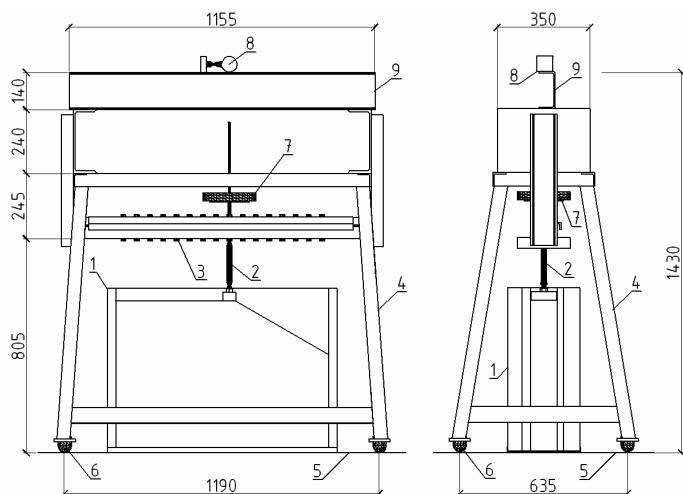


Fig. 4. Plan of the tester for flat deformation: 1 — tray; 2 — the loading device; 3 — frame plug; 4 — frame; 5 — table of the basement; 6 — adjusting screws; 7 — flat weights; 8 — deflectometer; 9 — cross bar

The experiments on loading the strengthened slopes in the given tray were carried out by author of the article under supervision of S. A. Pavlyushchik and N. M. Bondarenko, a student of Master course.

This research work [7] presents the results of numerous experiments on loading unreinforced slopes of various inclinations, including the ones of experiments with 30° sandy slopes.

The results of the experiments on loading 30° sandy slopes reinforced in 20 mm intervals by polythene horizontal layers (in double) are presented in the paper. Geometrical and physical conditions of modeling were met.

The loading was carried out gradually by 6 kg. On each step certain time was given for consolidation of the basement, and then yielding of foundation model were being fixed. The reinforced slope was brought to destruction, and limit load was defined.

Fig. 5 shows diagram of relation of yielding of foundation model on reinforced 30° slope to load in experiment № 7. For comparison in the same figure the corresponding diagram for unreinforced slope [7] is presented. The destructive load (fig. 6) on the reinforced slope in 204 kg has exceeded that on unreinforced slope as many as four times.

First, results of the experiments carried out will allow designers to make economically reasonable decisions, for example, in road construction.

Secondly, to apply correctly force in geosynthetics in calculating estimations of bearing capacity [6].

Strictly speaking, theoretically the lower bound estimations in the work [6] are derived for the continuous weightless environment, anisotropic on resistance to shear. Such continuous environment was modeling the composit environment: dense sand interlaid with geosynthetics. This or that purpose of cohesion of the anisotropic continuous environment function on size of the limit force for short-term break of geosynthetics can deprive estimation of bearing capacity adjective "bottom".

It is necessary to say, that European practice recommends that when applying work load on geosynthetics the test rapture force for geosynthetics should be divided into a number of rates, each of which is more than one.

Dense sand dilates at shear deformation, and its resistance reaches maximum at certain shear deformation, followed by reducing the resistance. At such deformations in geosynthetics stressses are unlikely to reach the limit values. It is clear, that cohesion for the modeling anisotropic environment should be appointed on the reduced short-term experimental rapture loads on geosynthetics.

Standard tests on stretching 2,5 sm width polythene strips have shown the rapture load of 0,9 kg. The double strip has limit rapture effort in 1,8 kg. Hence, the composite environment (2 sm thickness layer of condensed sand interlaid with double polythene layers) having horizontal direction will show cohesion. Its size on each rectangular 2,5 sm × 2 sm = 5 sm² is equal to 1,8 kg. Consequently, equivalent cohesion in a horizontal direction $c = 0,36 \text{ kg/sm} = 36 \text{ kPa}$. For the above reasons to calculate the estimation of bearingability using technique [6], specific cohesion in 70 % from short-term rapture load, i. e. $c = 25,2 \text{ kPa}$ be taken.

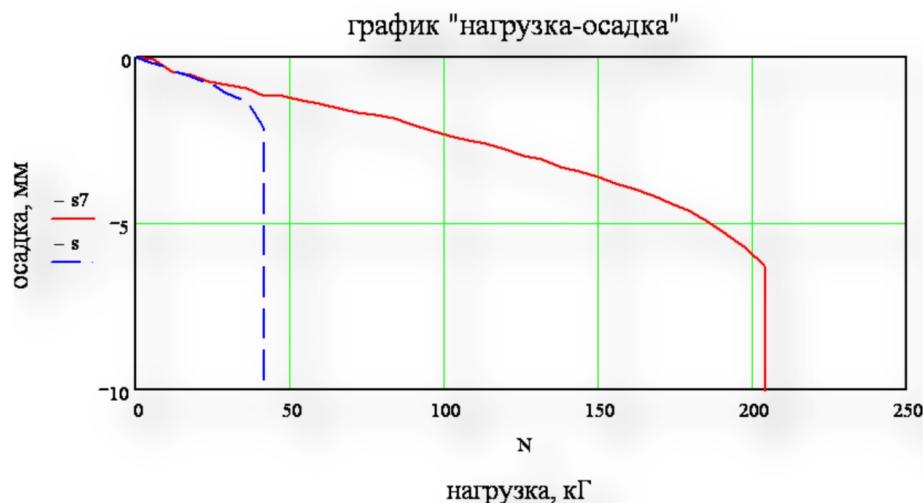


Fig. 5. Results of experiments on loading reinforced (a continuous line) and unreinforced (a dashed line) slopes

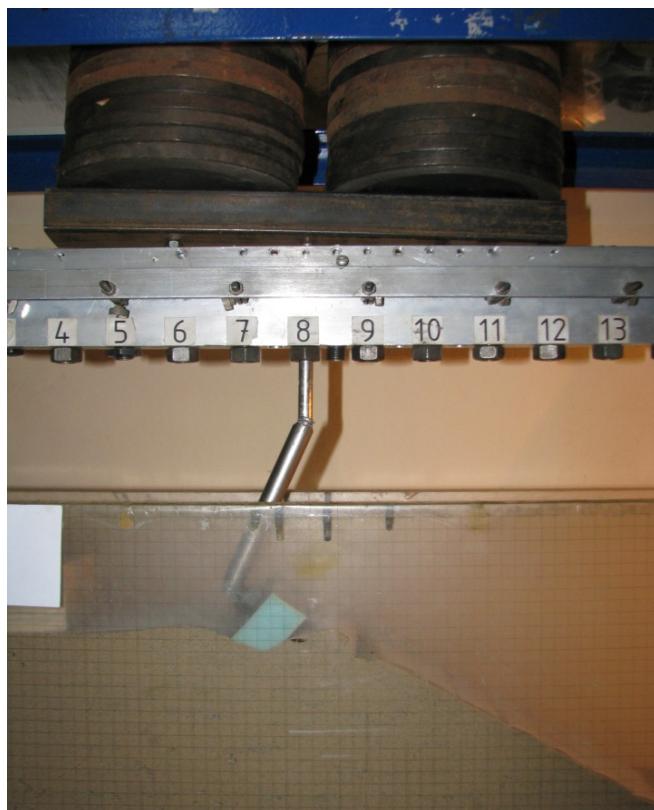


Fig. 6. Destruction of reinforced slope

Further, we shall study theoretical calculation of bearing capacity for model tests conditions. The algorithm of calculation is presented here, too.

ESTIMATIONS OF TESTLIMIT LOADS

Characteristics of the modeling anisotropic environment:

$$\varphi := \frac{\pi \cdot 40}{180} \quad \text{-- angle of internal friction}$$

$c := 0.025$ 2 MPa -- specific cohesion

$$C1 := \frac{2 \cdot c \cdot \cos(\varphi)}{1 - \sin(\varphi)}$$

$$A1 = 4.599 \quad A0 := A1 \quad C0 := 0 \quad \text{MPa} \quad C1 := 0.108 \quad \text{MPa}$$

$$A(\theta) = 2 \cdot \frac{\theta \cdot (A1 - A0)}{\pi} + A0 \quad C(\theta) = 2 \cdot \frac{\theta \cdot (C1 - C0)}{\pi} + C0$$

A add load $q := 0 \quad \text{MPa}$

$$m(\theta, g) = \sqrt{\left[(A1 - A0) \cdot \frac{2 \cdot q}{\pi} \right] - \left[(C1 - C0) \cdot \frac{2}{\pi} \right]^2 + 4 \cdot A(\theta) \cdot [(A(\theta) - 1) \cdot g - C(\theta)]^2}$$

$$f(\theta, g) := \frac{(C1 - C0) \cdot \frac{2}{\pi} - (A1 - A0) \cdot \frac{2 \cdot q}{\pi} - m(\theta, g)}{2 \cdot A(\theta)}$$

$$\theta0 := 0 \quad \theta1 := \frac{\pi}{2} \quad g0 := -q$$

$$\text{Corner of slope: } \alpha := \frac{\pi \cdot 30}{180} \quad \alpha = 0.524$$

$$m(t, y) = \left[(A1 - A0) \cdot \frac{2 \cdot y}{\pi} \right] - \left[(C1 - C0) \cdot \frac{2}{\pi} \right]^2 + 4 \cdot A(t) \cdot [(A(t) - 1) \cdot y - C(t)]^2$$

This QuickSheet can be used to solve an ordinary differential equation of the form:

$$\frac{dy}{dt} = f(t, y) \quad y(t0) = y0$$

Enter the initial value problem specifics:

$$t0 := \alpha \quad y0 := -q$$

Enter the desired solution parameters:

$$f(t, y) := \frac{(C1 - C0) \cdot \frac{2}{\pi} - (A1 - A0) \cdot \frac{2 \cdot y}{\pi} - \sqrt{m(t, y)}}{2 \cdot A(t)}$$

Endpoint of solution interval

$$t1 := \frac{\pi}{2}$$

Number of solution values on $[t0, t1]$

$$N := 1000$$

Given

$$y(t) = f(t, y(t)) \quad y(t0) = y0$$

$$y := \text{Odesolve}(t, t1)$$

$$y\left(\frac{\pi}{2}\right) = -0.064$$

Limit pressure upon the anisotropic basement

$$p := C\left(\frac{\pi}{2}\right) - y\left(\frac{\pi}{2}\right) \cdot A\left(\frac{\pi}{2}\right) \quad p = 0.400 \quad \text{MPa}$$

Limit pressure by Prandtl on the isotropic basement

$$p0 := A0 \cdot e^{\frac{(\frac{\pi}{2} - \alpha) \cdot (A0 - 1)}{\sqrt{A0}}} \cdot \left(q + \frac{C0}{A0 - 1} \right) - \frac{C0}{A0 - 1} \quad p0 = 0 \quad \text{MPa}$$

$$p1 := A1 \cdot e^{\frac{(\frac{\pi}{2} - \alpha) \cdot (A1 - 1)}{\sqrt{A1}}} \cdot \left(q + \frac{C1}{A1 - 1} \right) - \frac{C1}{A1 - 1} \quad p1 = 0.771 \quad \text{MPa}$$

$$s := 50 \quad \text{CM}^2 \quad N := 10 \cdot p \cdot s \quad \text{kN}$$

Limit force on foundation model: $N = 200.093 \quad \text{kN}$

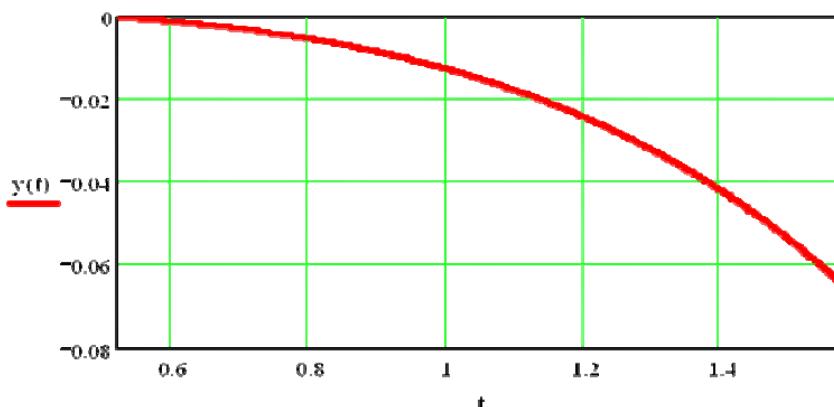


Fig. 7. The diagram of solution for Koshi's problem

Calculations have shown, that theoretical 200,1 kg limit load gives good conformity with test limit load of 204 kg.

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